

# **Search for Partonic EoS in High-Energy Collisions**

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**Many Thanks to Organizers!**

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# Outline

- **Motivation**
- **Bulk properties -  $\partial P_{QCD}$** 
  - Hadron spectra and elliptic flow
  - NCQ scaling: deconfinement
  - Heavy flavor collectivity: thermalization
- **Summary & Outlook**

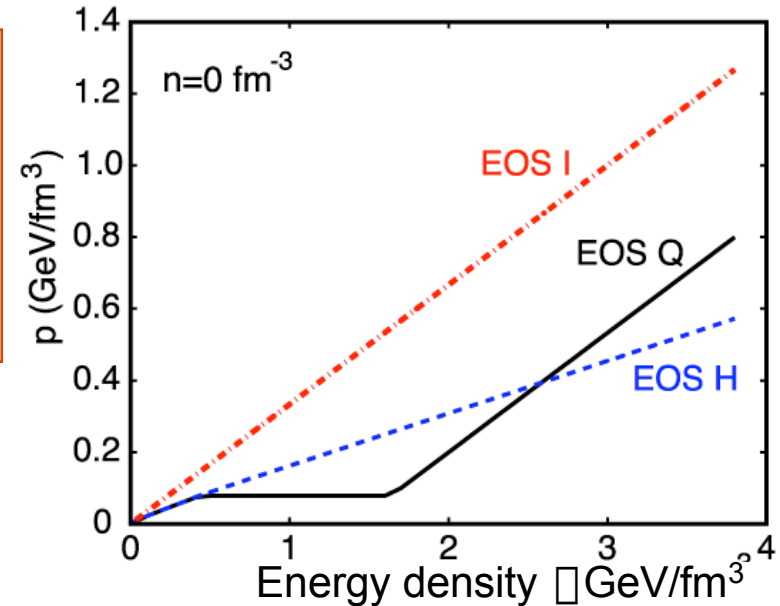
# Equation of State

$$\partial_\mu T^{\mu\mu} = 0$$

$$\partial_\mu j^\mu = 0 \quad j^\mu(x) = n(x)u^\mu(x)$$

$$T^{\mu\mu} = [\epsilon(x) + p(x)]u^\mu u^\mu - g^{\mu\mu} p(x)$$

With given degrees of freedom, the EOS - the system response to the changes of the thermal condition - is fixed by its  **$p$**  and  **$T(\epsilon)$** .



Equation of state:

- **EOS I** : relativistic ideal gas:  $p = \epsilon/3$
- **EOS H** : resonance gas:  $p \sim \epsilon/6$
- **EOS Q** : Maxwell construction:  
 $T_{\text{crit}} = 165 \text{ MeV}$ ,  $B^{1/4} = 0.23 \text{ GeV}$   
 $\epsilon_{\text{lat}} = 1.15 \text{ GeV/fm}^3$

*P. Kolb et al., Phys. Rev. **C62**, 054909 (2000).*

# Pressure, Flow, ...

$$d\epsilon = dU + pdV$$

$\epsilon$  – entropy;  $p$  – pressure;  $U$  – energy;  $V$  – volume  
 $\epsilon = k_B T$ , thermal energy per dof

In high-energy nuclear collisions, *interaction* among *constituents* and *density distribution* will lead to:

***pressure gradient***  $\Rightarrow$  ***collective flow***

- $\epsilon$  number of degrees of freedom (dof)
- $\epsilon$  Equation of State (EOS)
- $\epsilon$  No thermalization is needed – pressure gradient only depends on the ***density gradient and interactions***.
- $\epsilon$  Space-time-momentum correlations!

# Collectivity, Local thermalization

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# High-energy Nuclear Collisions

## Initial Condition

- initial scatterings
- baryon transfer
- $E_T$  production
- parton dof

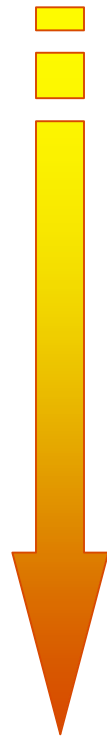
## System Evolves

- parton interaction
- parton/hadron expansion

## Bulk Freeze-out

- hadron dof
- interactions stop

$Q^2$



*time*

*jets*

partonic scatterings?  
early thermalization?

$J/\psi$ ,  $D$



$\pi$ ,  $K$ ,  $K^*$

$\pi$ ,  $p$

$d$ , HBT

*elliptic flow  $v_2$*



*radial flow  $\langle \beta_T \rangle$*

$T_c$   
 $T_{ch}$

$T_{fo}$

# High-energy Nuclear Collisions

## Initial Condition

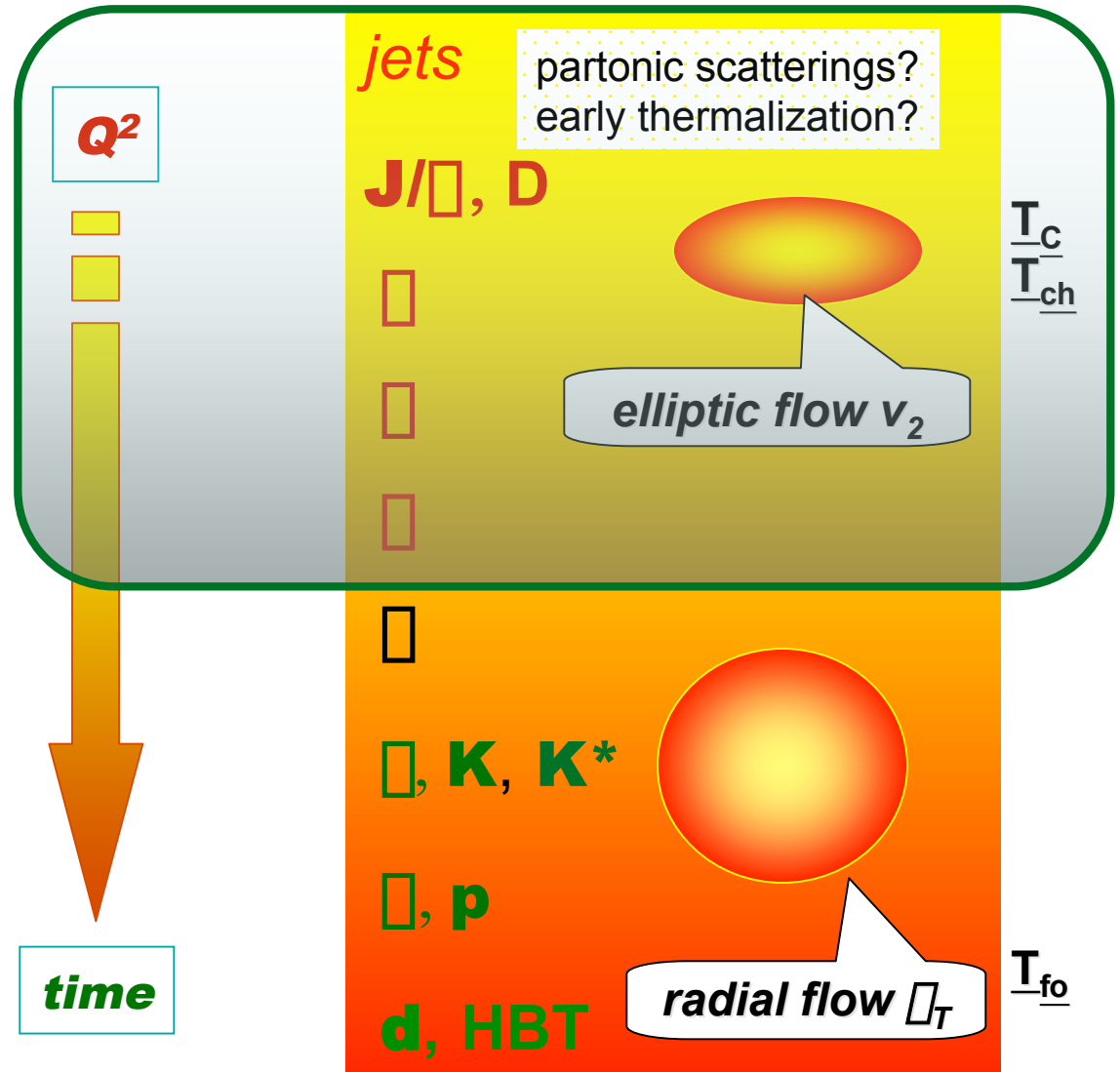
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# Transverse Flow Observables

$$\frac{dN}{p_t dp_t dy d\phi} = \frac{1}{2\pi} \frac{dN}{p_t dp_t dy} + \sum_{i=1}^{\infty} 2v_i \cos(i\phi)$$

$$p_t = \sqrt{p_x^2 + p_y^2}, \quad m_t = \sqrt{p_t^2 + m^2}$$

As a function of particle mass:

- Directed flow ( $v_1$ ) – early *see Markus Oldenburg's talk*
- Elliptic flow ( $v_2$ ) – early
- Radial flow – integrated over whole evolution

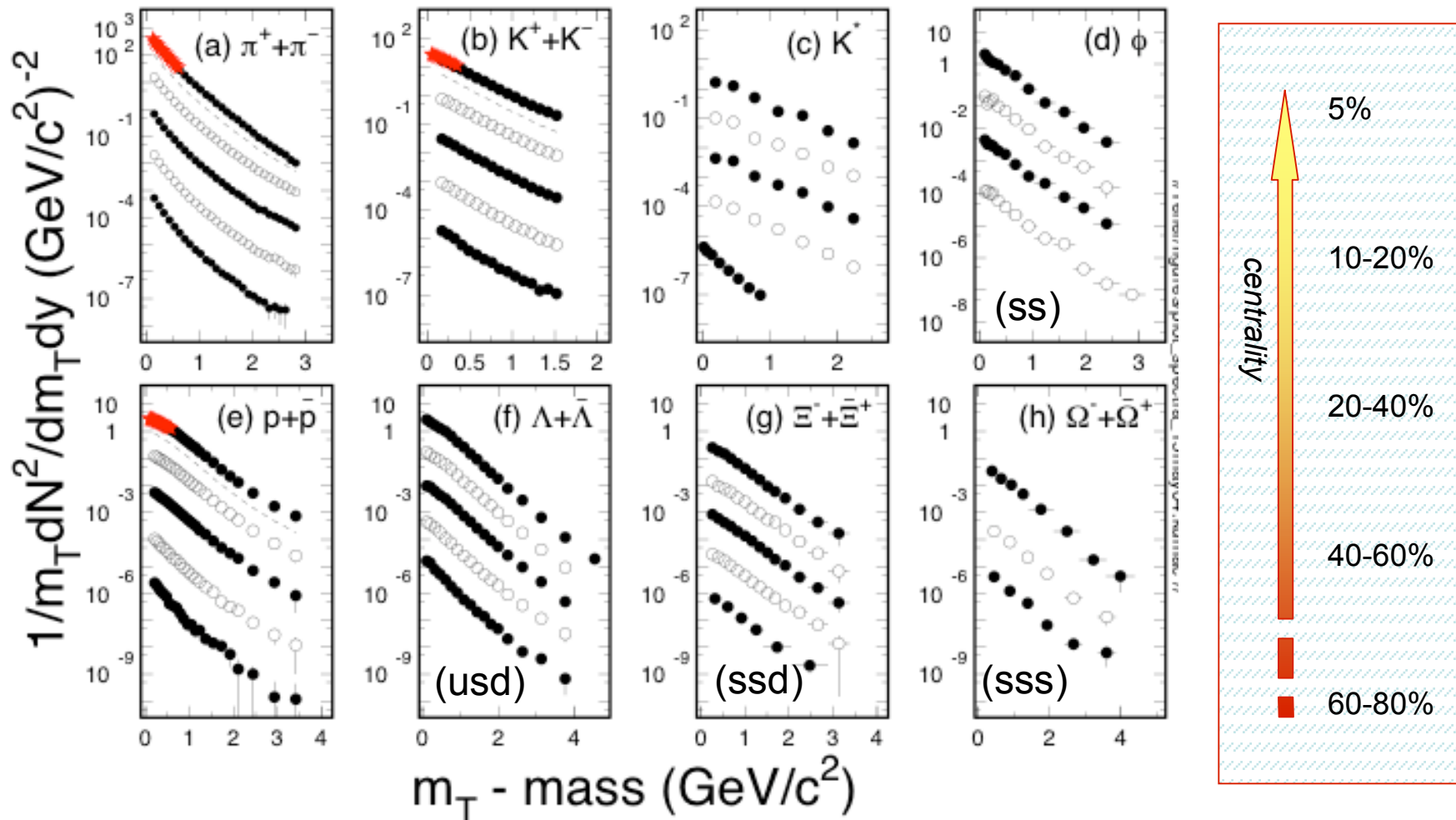
Note on collectivity:

- 1) Effect of collectivity is accumulative – final effect is the sum of all processes.
- 2) Thermalization is not needed to develop collectivity - pressure gradient depends on **density gradient** and **interactions**.



# Hadron Spectra from RHIC

mid-rapidity,  $p+p$  and  $Au+Au$  collisions at 200 GeV



$$m_T = \sqrt{p_T^2 + m^2}$$

Results from BRAHMS, PHENIX, and STAR experiments

# Thermal model fit

Source is assumed to be:

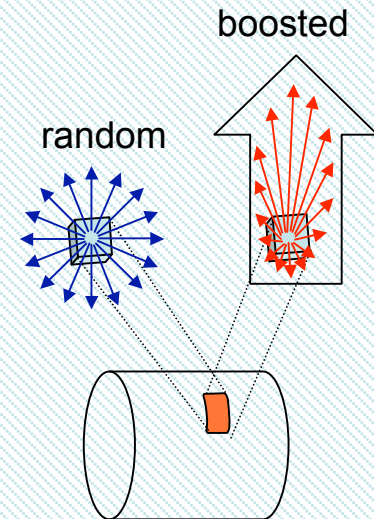
- Local thermal equilibrated
- Boosted radially

*E. Schnedermann, J. Sollfrank, and U. Heinz, Phys. Rev. **C48**, 2462(1993)*

$$E \frac{d^3 N}{dp^3} \mu \int_0^R e^{-(u^\parallel p^\parallel)/T_{fo}} p d\phi \int_0^{\phi_0} d\phi$$

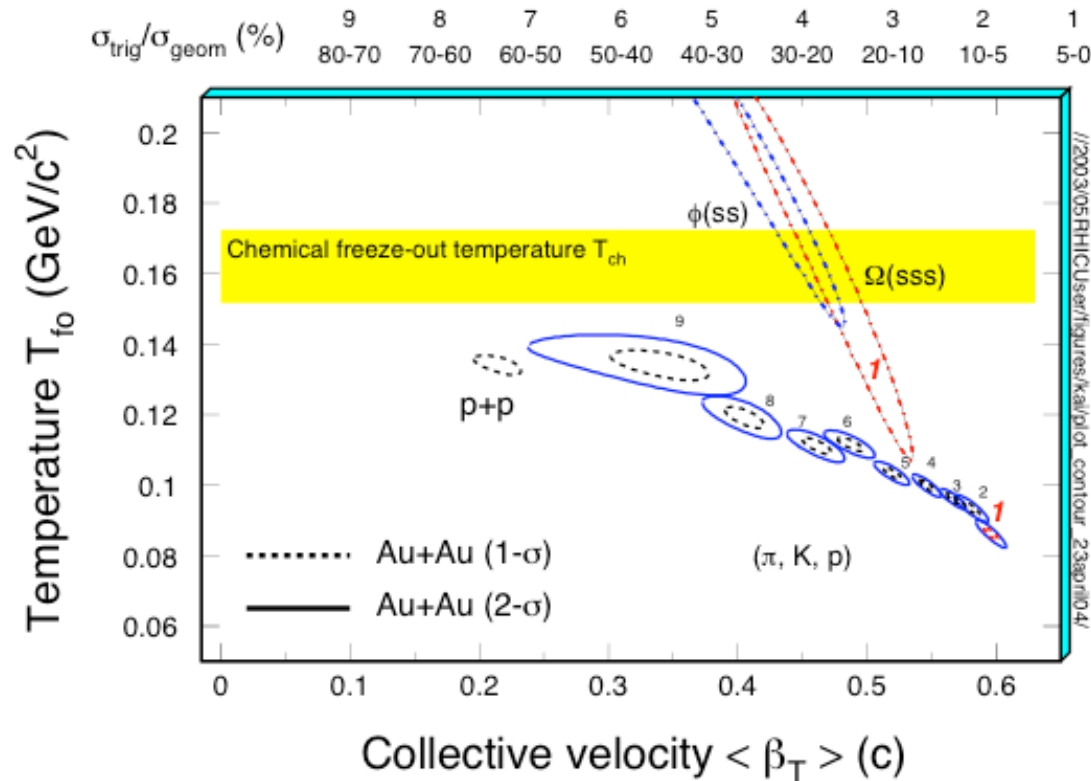
$$\frac{dN}{m_T dm_T} \mu \int_0^R r dr m_T K_1 \left[ \frac{m_T \cosh \phi}{T_{fo}} \right]_0^{\phi_0} \left[ \frac{p_T \sinh \phi}{T_{fo}} \right]_0^{\phi_0}$$

$$\phi = \tanh^{-1} \beta_r \quad \beta_r = \frac{r}{R} \quad \phi = 0.5, 1, 2$$



# Thermal fits: $T_{fo}$ vs. $\langle \beta_T \rangle$

## 200GeV Au + Au collisions



Chemical Freeze-out: inelastic interactions stop  
Kinetic Freeze-out: elastic interactions stop

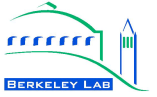
- 1)  $\pi$ ,  $K$ , and  $p$  change smoothly from peripheral to central collisions.
- 2) At the most central collisions,  $\langle \beta_T \rangle$  reaches 0.6c.
- 3) Multi-strange particles  $\phi$ ,  $\Omega$  are found at higher  $T_{fo}$  ( $T \sim T_{ch}$ ) and lower  $\langle \beta_T \rangle$

⇒ **Sensitive to early partonic stage!**

⇒ **How about  $v_2$ ?**

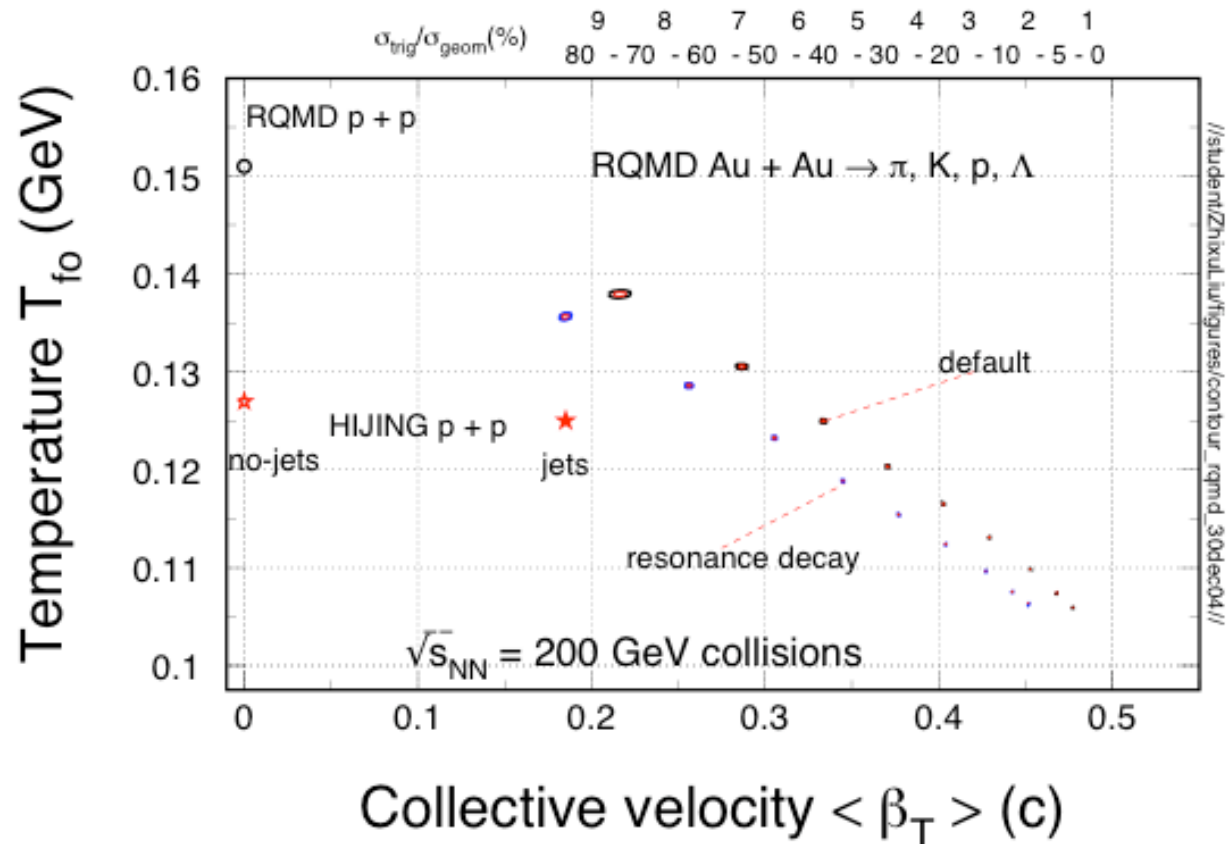
Data: STAR: NP **A715**, 458c(03); PRL **92**, 112301(04); **92**, 182301(04).  
NA49: nucl-ex/0409004

Chemical fits: Braun-Munzinger, Redlich, Stachel, nucl-th/0304013



//Talk/2005/01Hirscheegg05//

# Resonance decay tests

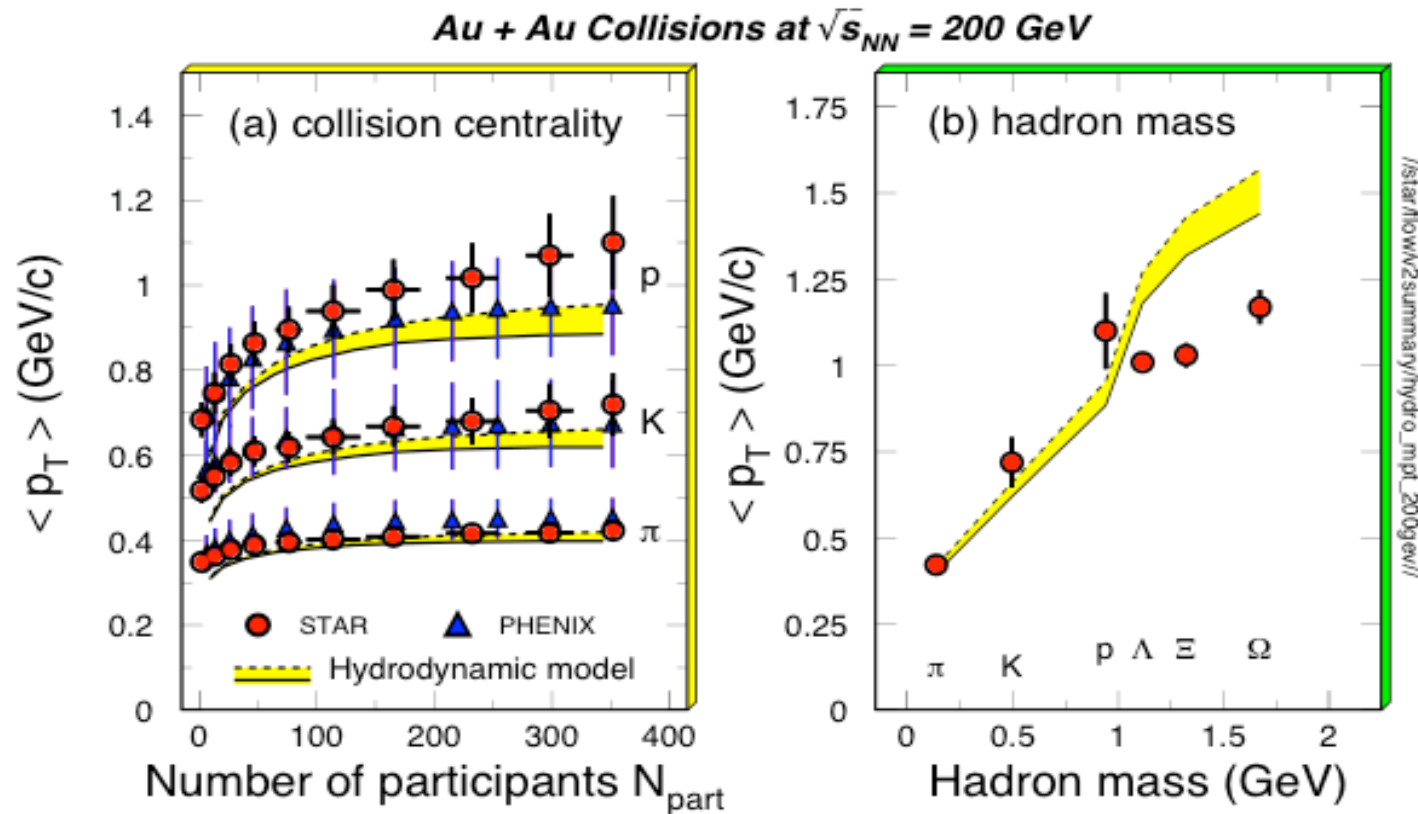


(1) Resonance decay of  $\rho$ ,  $\omega$ ,  $\phi$ ,  $\eta$  do not affect the freeze-out properties - there are life after the chemical freeze-out!

(2) 'Jets' lead to finite in p+p collisions

Zhixu Liu et al., December 2004.

# Compare with Model Results



Model results fit to  $\pi$ , K, p spectra well, but over predicted  $\langle p_T \rangle$  for multi-strange hadrons - **Do they freeze-out earlier?**

*Phys. Rev.* **C69** 034909 (04); *Phys. Rev. Lett.* **92**, 112301(04); **92**, 182301(04); P. Kolb et al., *Phys. Rev.* **C67** 044903(03)

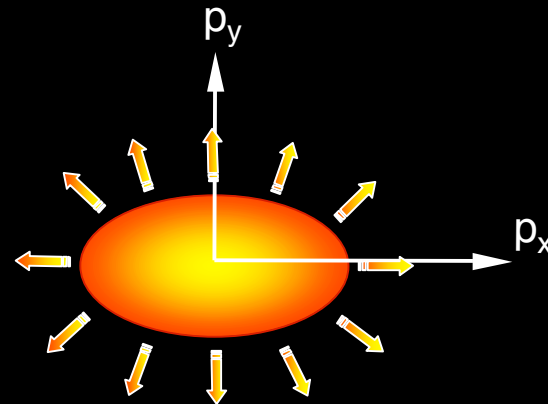
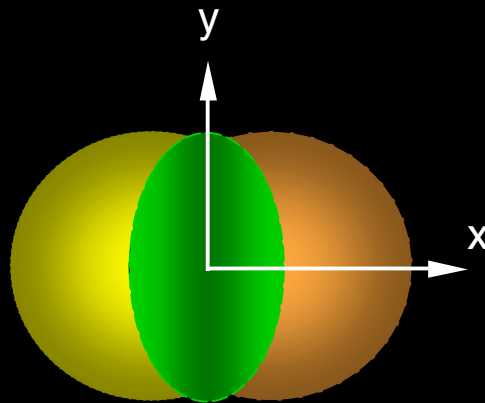


# Anisotropy Parameter $v_2$

coordinate-space-anisotropy



momentum-space-anisotropy

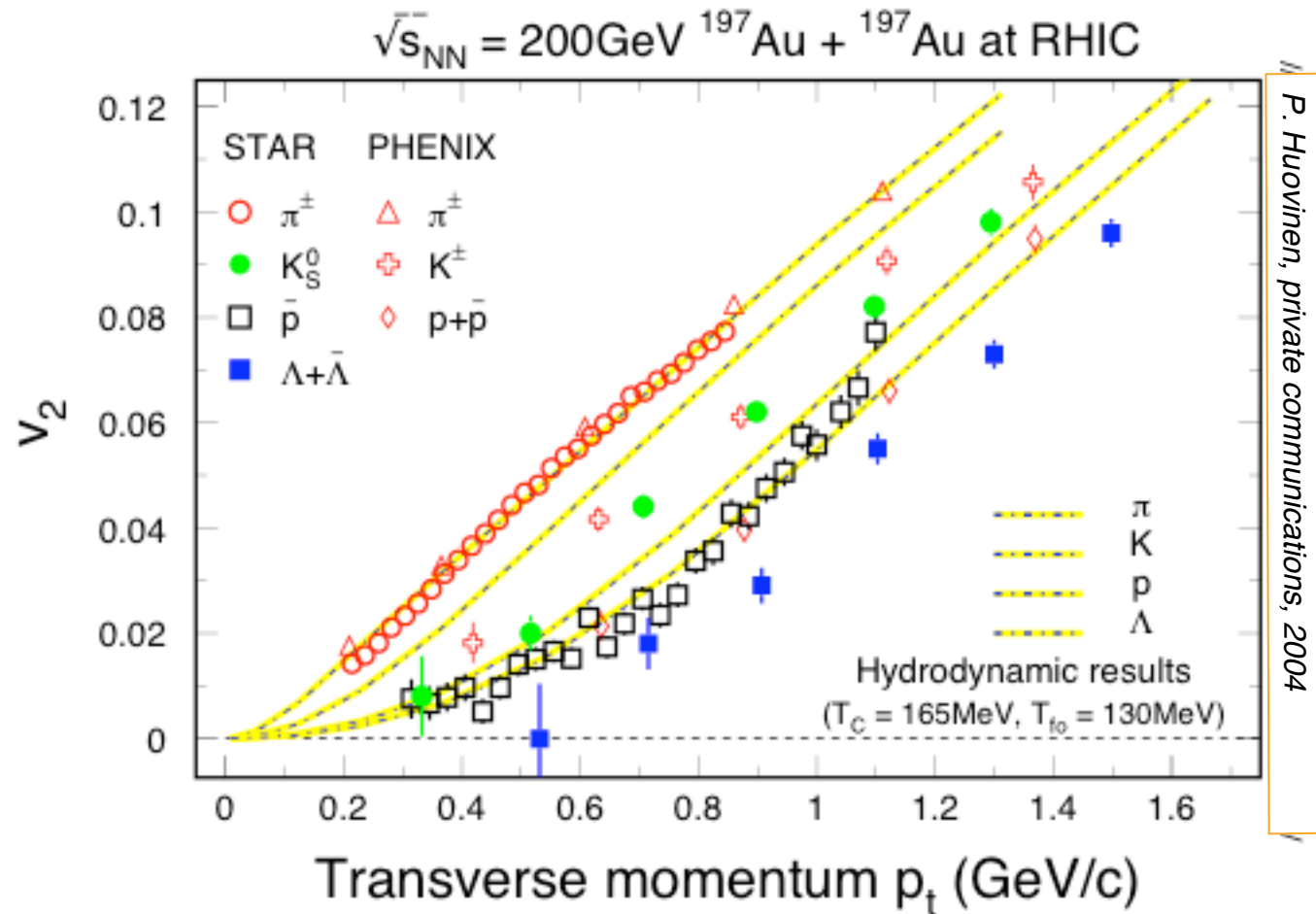


$$\phi = \frac{y^2 - x^2}{y^2 + x^2}$$

$$v_2 = \langle \cos 2\phi \rangle, \quad \phi = \tan^{-1} \left( \frac{p_y}{p_x} \right)$$

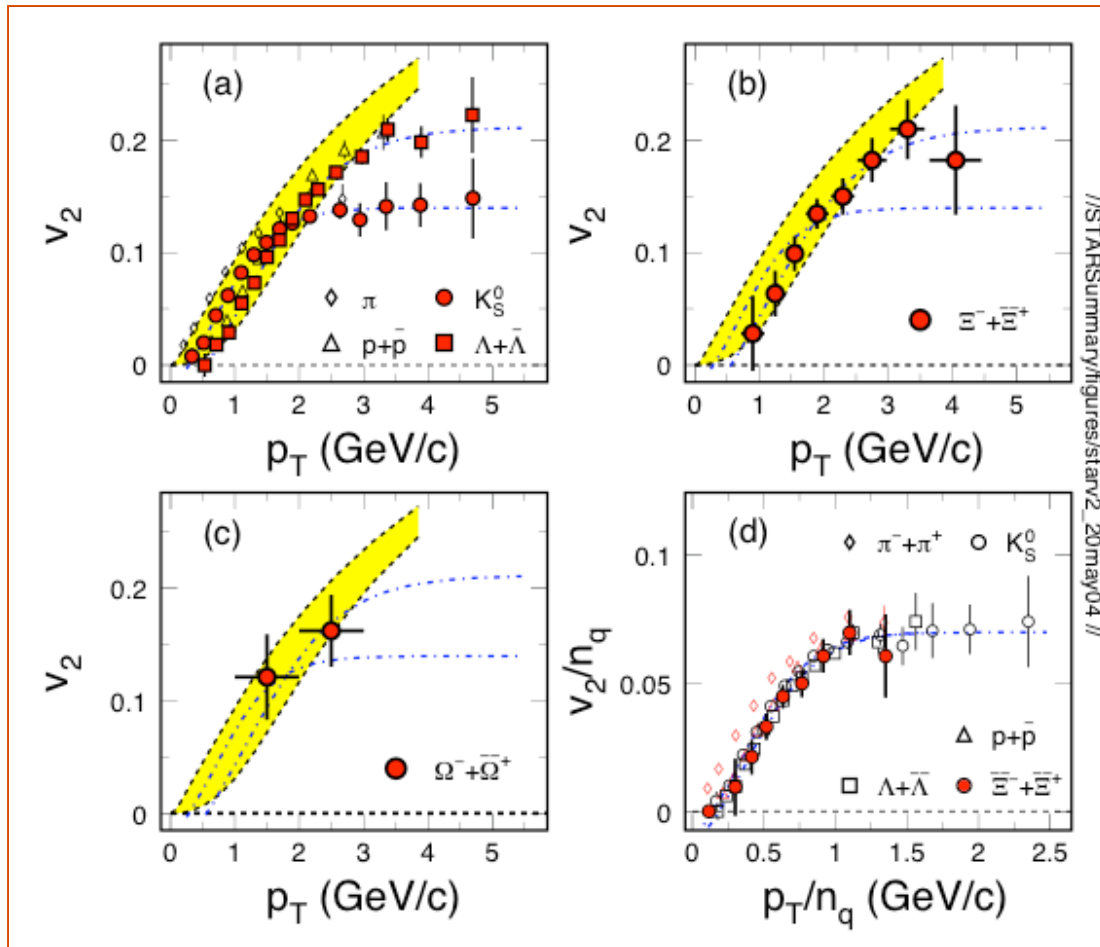
**Initial/final conditions, EoS, degrees of freedom**

# $v_2$ at low $p_T$ region



- Minimum bias data! At low  $p_T$ , model result fits mass hierarchy well!
- Details does not work, need more flow in the model!

# $v_2$ at all $p_T$



- $v_2$ , spectra of light hadrons and multi-strange hadrons
- scaling of the number of constituent quarks

At RHIC:

⇒ **Partonic collectivity has been attained**

⇒ **Deconfinement has been attained**

PHENIX: PRL**91**, 182301(03)

STAR: PRL**92**, 052302(04)

S. Voloshin, NPA**715**, 379(03)

Models: Greco et al, PRC**68**, 034904(03)

X. Dong, et al., Phys. Lett. **B597**, 328(04).

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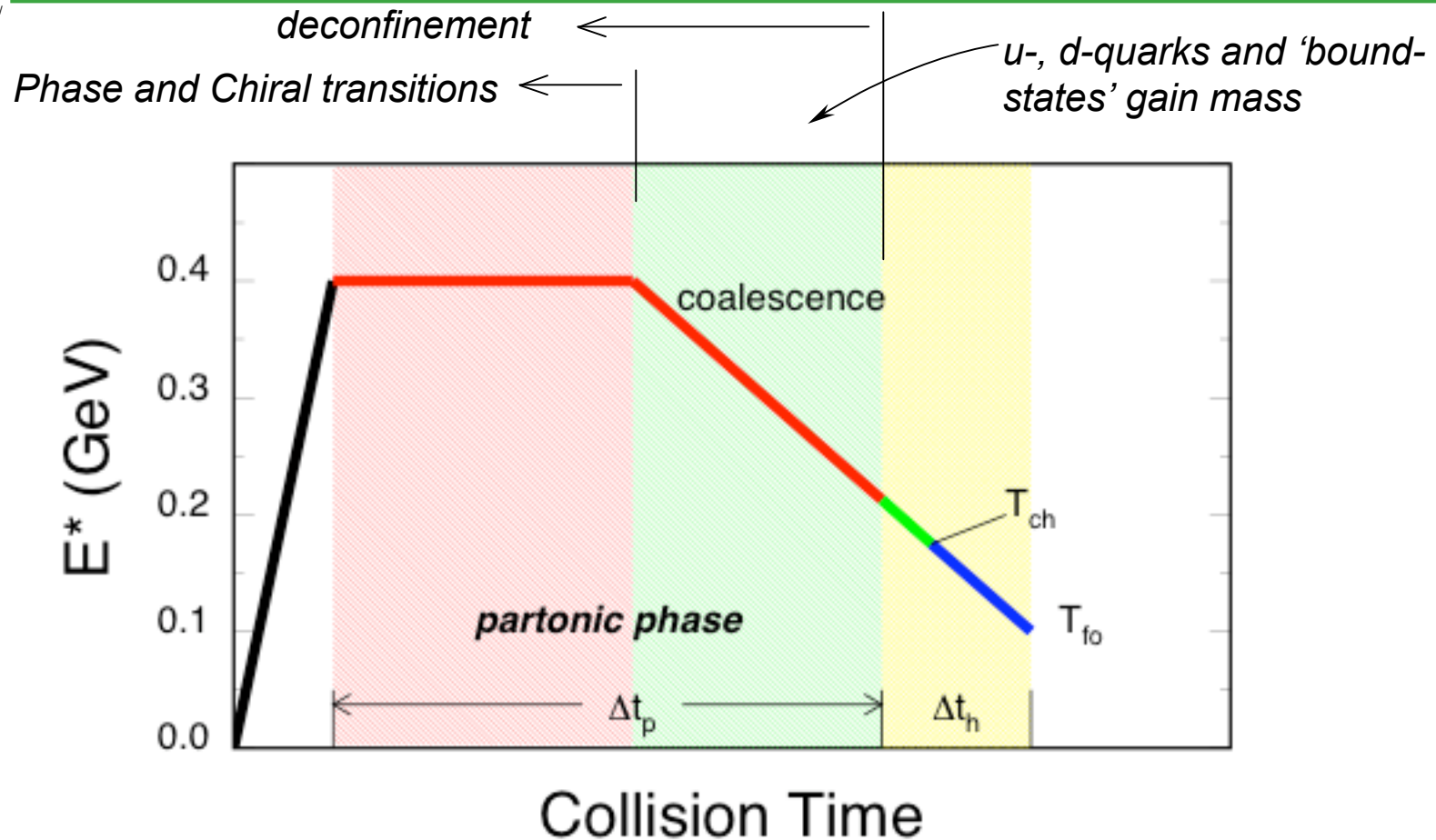


# Partonic Collectivity at RHIC

- 1) Copiously produced hadrons freeze-out:  
 $T_{fo} = 100 \text{ MeV}, \quad \beta_T = 0.6 (c) > \beta_T(\text{SPS})$
- 2)\* Multi-strange hadrons freeze-out:  
 $T_{fo} = 160\text{-}170 \text{ MeV} (\sim T_{ch}), \quad \beta_T = 0.4 (c)$
- 3)\*\* Multi-strange  $v_2$ :  
**Multi-strange hadrons  $\beta$  and  $\beta$  flow!**
- 4)\*\*\* Constituent Quark scaling:  
Seems to work for  $v_2$  and  $R_{AA}$  ( $R_{CP}$ )

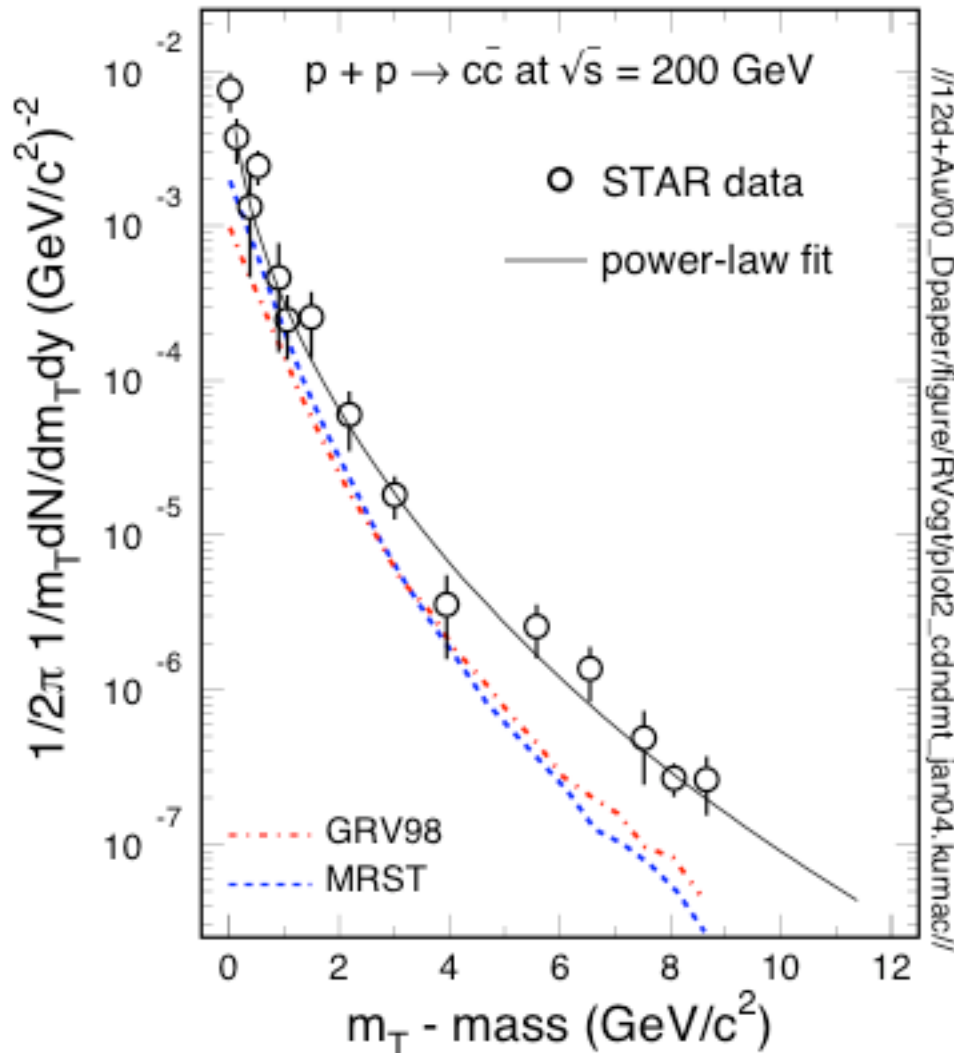
**Deconfinement**  
**Partonic (*u,d,s*) Collectivity**

# Time Scale



- 1) Coalescence processes occur during phase transition and hadronization;
- 2) The  $u$ -,  $d$ -quarks and 'bound-states' gain mass accompanied by expansion;
- 3) Early thermalization with partons and its duration need to be checked.

# Open charm production at RHIC



- First reconstructed open charm spectrum at RHIC

Model:

- pQCD distributions are steeper
- Fragmentation with delta function has harder spectrum
- Total cross sections are lower, a factor of 3-5

- STAR data: A. Tai et al., J. Phys **G30**: S809(2004); nucl-ex/0404029
- model results: R. Vogt, 2004

# Charm production

1) STAR and PHENIX results are different:

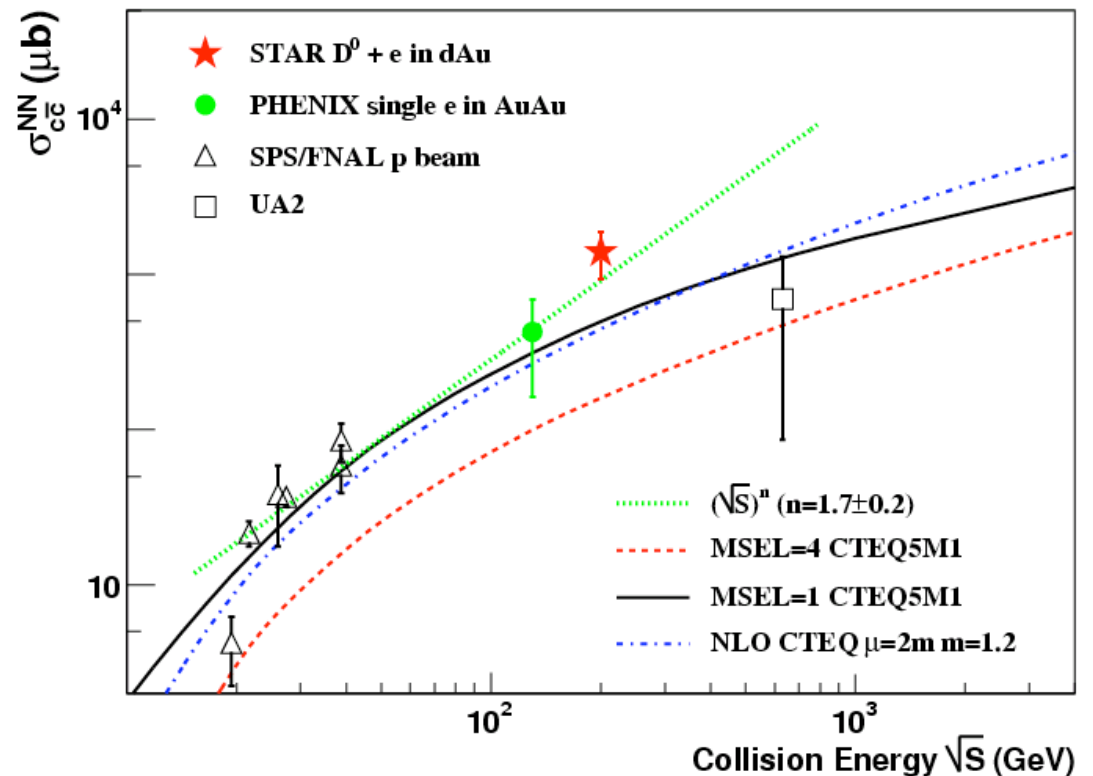
$$\sigma_{c\bar{c}}^{\text{total}} = 700 \text{ -- } 1200 (\mu\text{b})$$

2) NLO pQCD calculations under-predict the  $c\bar{c}$  production cross section at RHIC

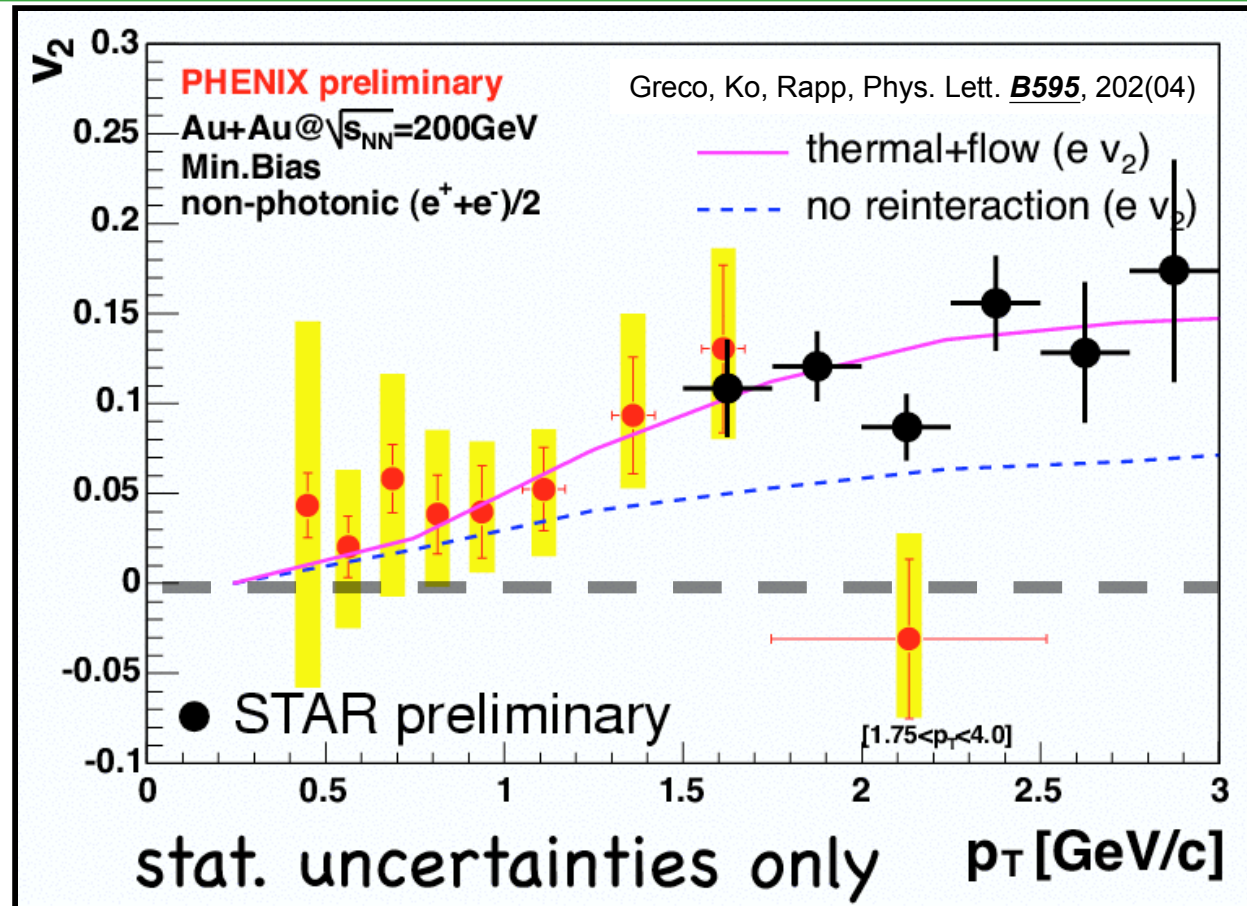
3) Power law for  $c\bar{c}$  cross section from SPS to RHIC:  
 **$n \sim 2$**   
 ( $n \sim 0.5$  for charged hadrons)

4) Large uncertainties in total cross section due to rapidity width, model dependent(?).

STAR data: PRL accepted, nucl-ex/0407006



# Non-photonic electron $v_2$

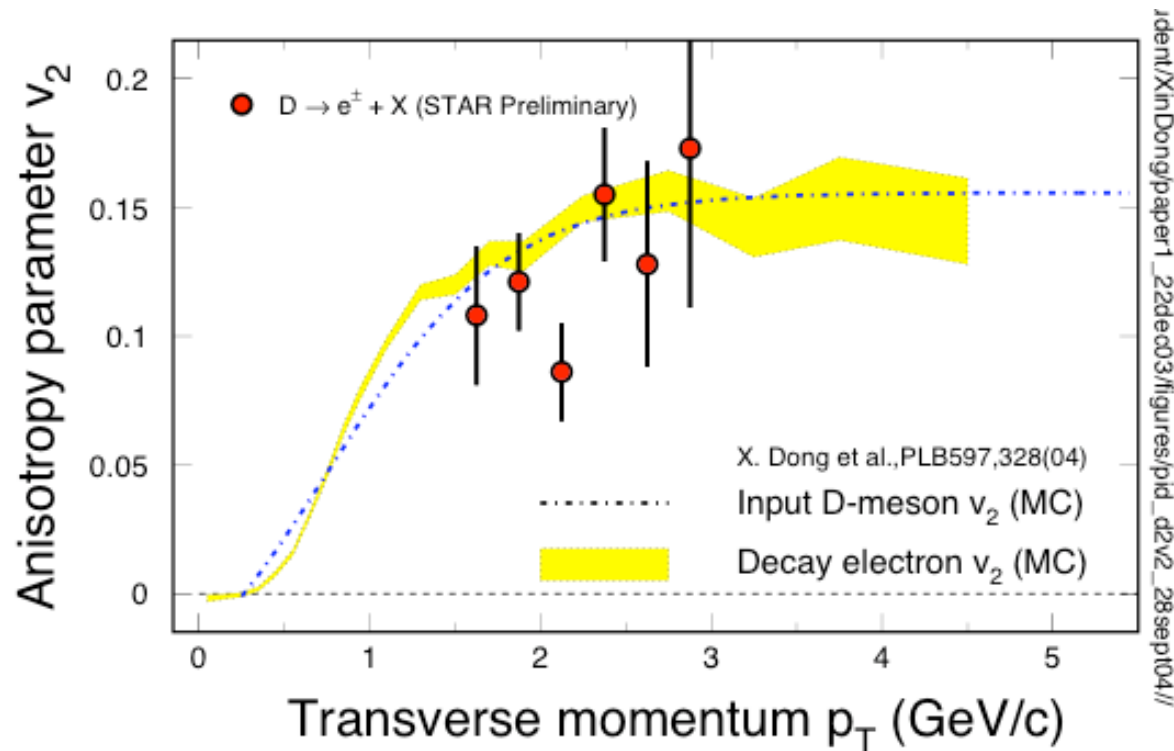


STAR: 0-80% (F.Laue SQM04)  
statistical error only  
corrected for  $e^\pm$  from  $\pi$  decay

PHENIX: Minimum bias

M. Kaneta *et al*, J.Phys. **G30**, S1217(04)

# Open charm $v_2$ - a comparison



- 1) Constituent Quark Scaling for open charm hadron production?
- 2) Flow of charm-quark and the thermalization among light flavors?
- 3) ...????

HSD: E. Bratkovskaya et al., hep-ph/0409071

X. Dong, S. Esumi, et al., Phys. Lett. **B597**, 328(2004).

# Summary & Outlook

(1) Collectivity - pressure gradient  $\partial P_{QCD}$

⇒ **Deconfinement and partonic collectivity at RHIC**

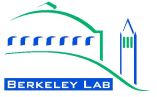
(2) Partonic ( **$u, d, s$** ) thermalization

- heavy flavor  $v_2$  and spectra
- di-lepton and thermal photon spectra
- $J/\psi$  production

(3)  $\sqrt{s}$ -vertex upgrades Phenix and STAR

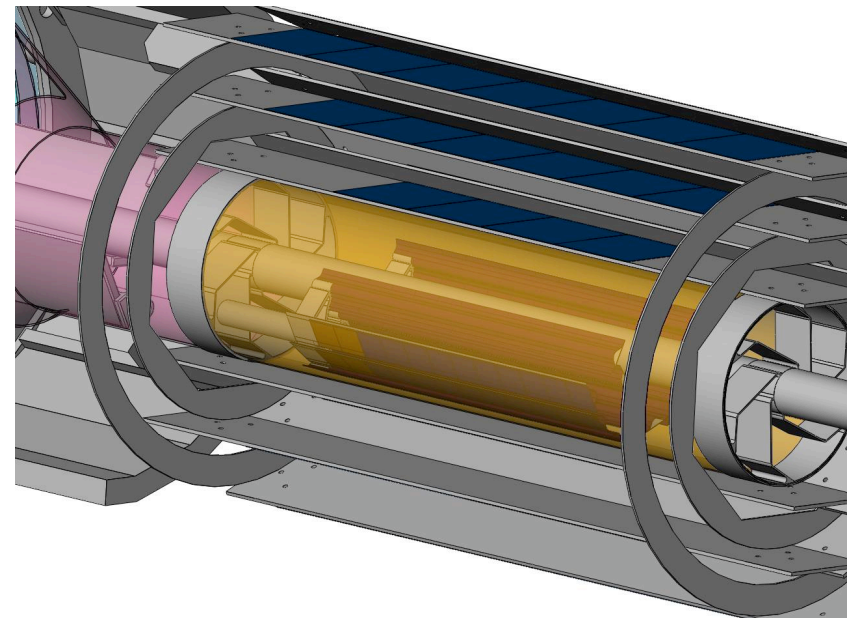
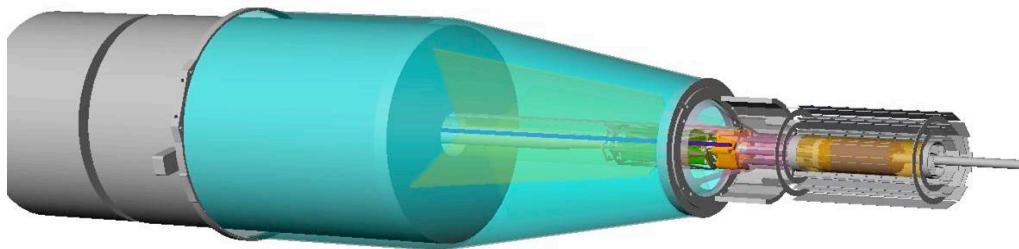
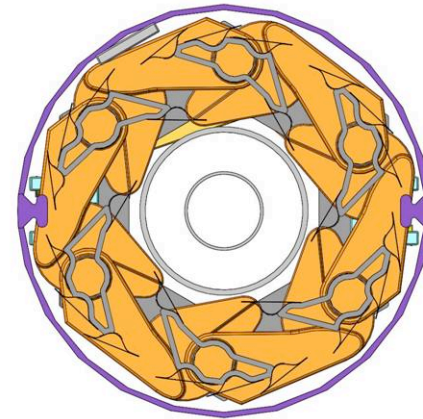
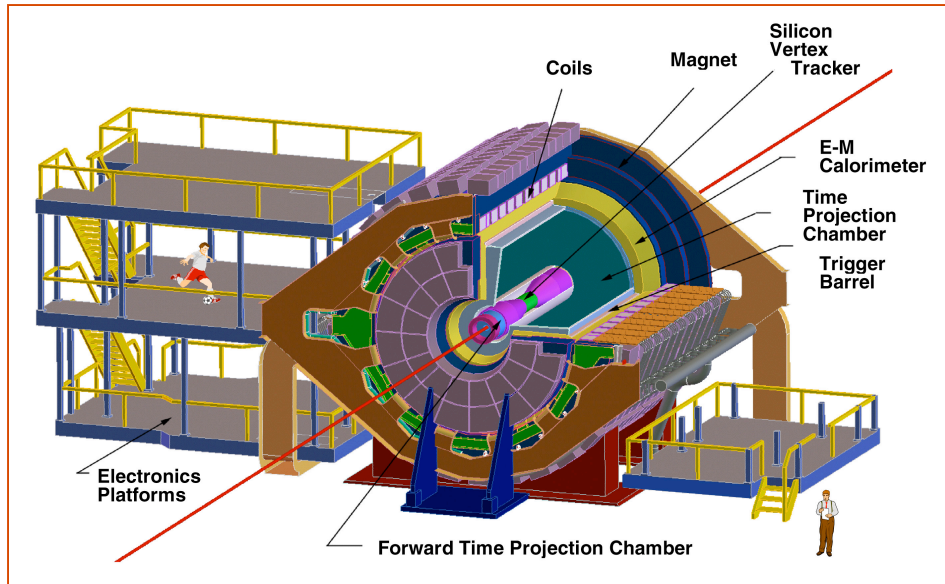
- open charm
- resonances with both hadronic & leptonic decays





//Talk/2005/01Hirscheegg05//

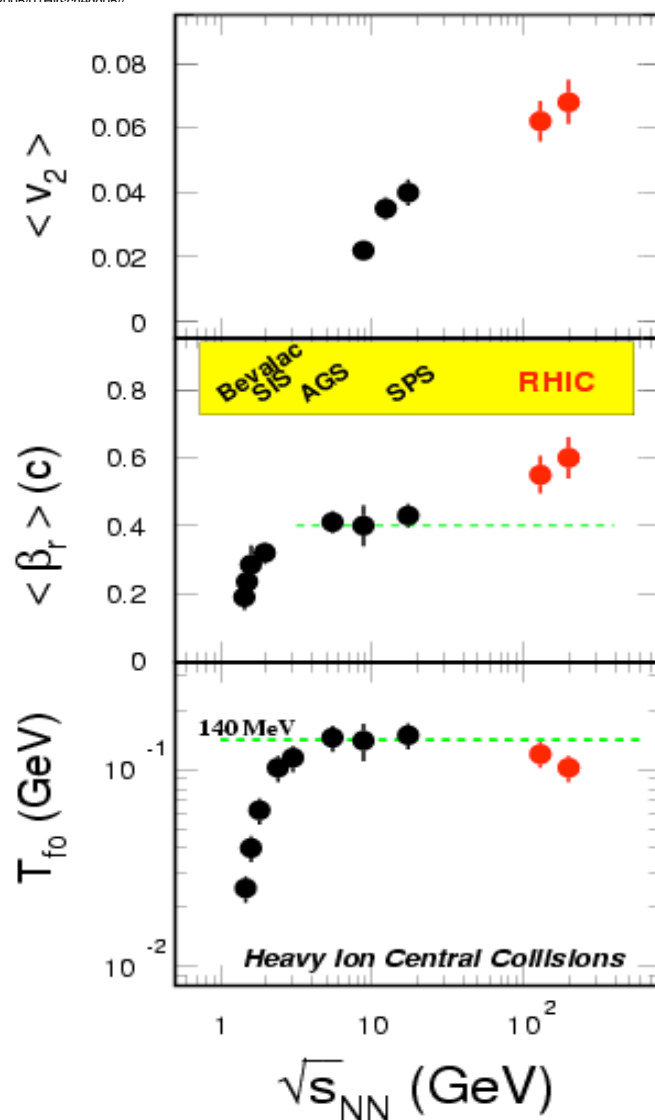
# STAR $\pi$ -vertex detector



*H. Wieman et al., STAR Collaboration*



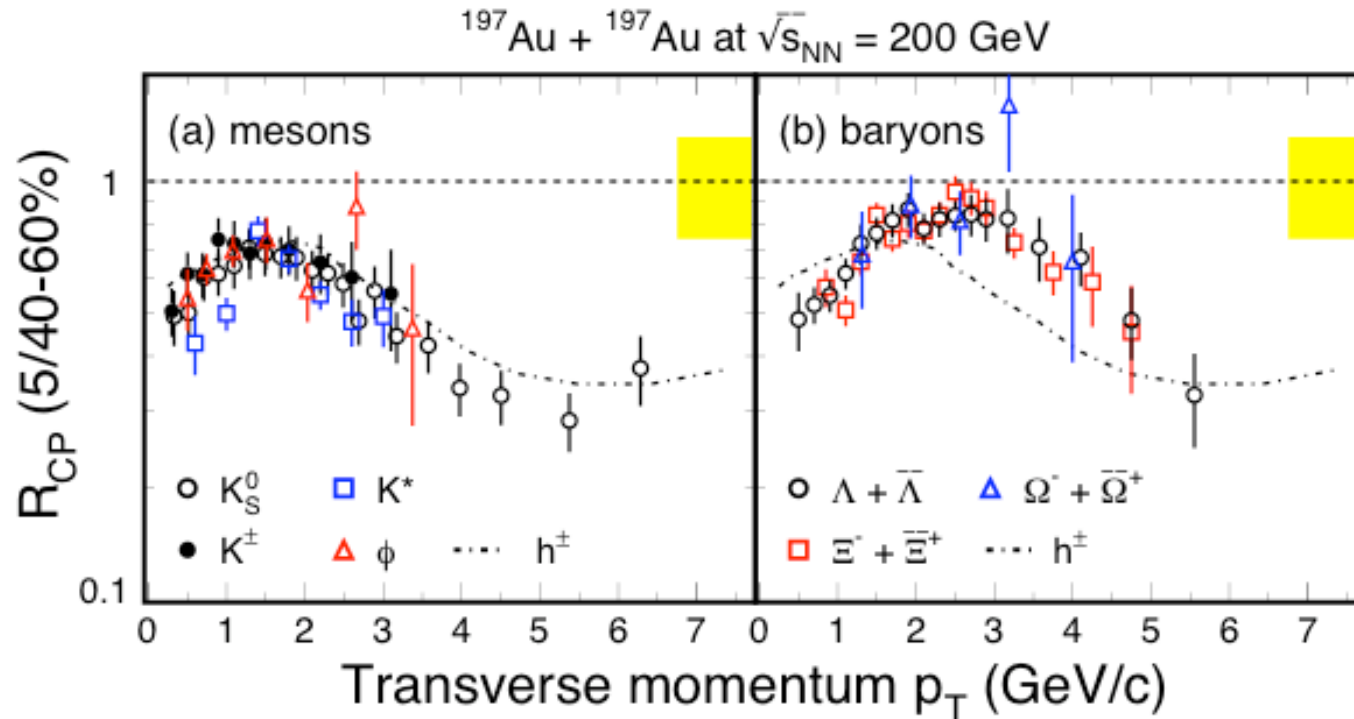
# Bulk Freeze-out Systematics



**The additional increase in  $\langle v_2 \rangle$  is likely due to partonic pressure at RHIC.**

- 1)  $v_2$  self-quenching, hydrodynamic model seem to work at low  $p_T$
- 2) Multi-strange hadron freeze-out earlier,  $T_{fo} \sim T_{ch}$
- 3) Multi-strange hadron show strong  $v_2$

# Nuclear Modification Factor



$$R_{\text{CP}}(p_T) = \frac{d^2 N^{\text{central}} / (N_{\text{binary}}^{\text{central}} dp_T dy)}{d^2 N^{\text{peripheral}} / (N_{\text{binary}}^{\text{peripheral}} dp_T dy)}$$

- ( $K^0$ ,  $\square$ ): PRL92, 052303(04); NPA715, 466c(03);
- Greco et al, PRC68, 034904(03); PRL90, 202102(03)
- R. Fries et al, PRC68, 044902(03); , Hwa, nucl-th/0406072

- 1) Baryon vs. meson effect!
- 2) Hadronization via coalescence
- 3) Parton thermalization (model)